

M.Sc.(Maths.) Semester - 1 (CBCS) Examination**Nov/Dec - 2022 [NEW COURSE]****Classical Mechanics 1(Elective (New))****Time: 2:30 Hours****Marks: 70****Instructions:**

1. All questions are compulsory.
2. Figures to the right indicate marks.

Q.1(A): Answer any one of following question. (04)

- (i) State and prove law of conservation of linear momentum for a particle.
- (ii) Prove that total virtual work done on a system of particle in equilibrium vanishes.

Q.1(B): Attempt any two out of three. (10)

- (i) Prove that Newton's equations of motion and Lagrange's equations of motion are same in absence of constraints.
- (ii) Define principle of virtual work and derive D'Alembert's principle.
- (iii) State Lagrange's equations of motion in general case and derive it for non-conservative force.

Q.2(A): Answer any one of following question. (04)

- (i) Define Hamiltonian's principle and derive Lagrange's equations of motion from it.
- (ii) Describe Brachistochrone problem (Problem of least time).

Q.2(B): Attempt any two out of three. (10)

- (i) In usual notations derive condition for extremum.
- (ii) State law of conservation of energy in Lagrangian formalism and using it show that energy is conserved for Simple Harmonic Oscillator.
- (iii) Obtain the curve for minimum surface of revolution.

Q.3(A): Answer any one of following question. (04)

- (i) State and prove Euler's theorem on motion of rigid body.
- (ii) Lagrangian of Simple Harmonic Oscillator is given by $L = \frac{m}{2} \dot{x}^2 - \frac{k}{2} x^2$. Obtain its Hamiltonian.

Q.3(B): Attempt any two out of three. (10)

- (i) Show that the central force motion of two bodies about their centre of mass can always be reduced to an equivalent one body problem.
- (ii) State and prove Kepler's third law of planetary motion.
- (iii) If a particle of mass m moves under a central force then its orbit is a plane curve.

Q.4(A): Answer any one of following question. (04)

- (i) Write any one effect of Coriolis force.
- (ii) Prove that the matrix for infinitesimal canonical transformation is symplectic.

Q.4(B): Attempt any two out of three. (10)

- (i) Derive Cayley-Klein parameters.
- (ii) Discuss in detail finite rotation.
- (iii) In usual notations derive the formula $d\mathbf{r} = \mathbf{r} \times d\boldsymbol{\Omega}$

Q.5(A): Answer any one of following question. (04)

- (i) Derive energy function.
- (ii) Define canonical transformation. Is the following transformation canonical? $Q_1 = q_1, P_1 = p_1 - 2p_2, Q_2 = p_2, P_2 = -2q_1 - q_2$

Q.5(B): Attempt any two out of three. (10)

- (i) Giving all details about Atwood's machine, derive Lagrange's equations of motion for it.
- (ii) State and prove Euler's theorem in motion of rigid body.
- (iii) Explain Eulerian angles.
